## Open4Tech Summer School 2019

All Things JavaScript Coding Pro-Practices
Curry On Functional Programming HTML, CSS \& JS in the Real World Java vs Python: Coding Deadmatch

OOP Techniques in a Simple Game
REST In Node.JS At The React \& Angular SPA
Sneak Peek Into Next Level QA (Test Automation)
Windows App Development with .NET WPF
You'll Neversea Algorithms Like These


## Open4Tech Summer School 2019

|  | Luni | Marti | Miercuri | Joi | Vineri |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | 24 iunie | 25 iunie | 26 iunie | 27 iunie | 28 iunie |
| 2-4pm | All Things JavaScript | All Things JavaScript | REST in Node.JS at the React \& Angular SPA | REST in Node.JS at the React \& Angular SPA | All Things JavaScript |
| 4-6pm | OOP Techniques in a Simple Game | OOP Techniques in a Simple Game | OOP Techniques in a Simple Game | Windows App Development with .NET WPF | Windows App Development with .NET WPF |
| 6-8pm | HTML, CSS \& JS in the Real World | HTML, CSS \& JS in the Real World | HTML, CSS \& JS in the Real World | Java vs Python: Coding Deathmatch | Java vs Python: Coding Deathmatch |
|  | 1 iulie | 2 iulie | 3 iulie | 4 iulie | 5 iulie |
| 2-4pm |  |  | REST in Node.JS at the React \& Angular SPA | REST in Node.JS at the React \& Angular SPA |  |
| 4-6pm | Coding Pro-Practices | Coding Pro-Practices | Coding Pro-Practices | You'll Neversea Algorithms Like These | You'll Neversea Algorithms Like These |
| 6-8pm | Java vs Python: Coding Deathmatch | Sneak Peek Into Next Level QA (Test Automation) | Sneak Peek Into Next Level QA (Test Automation) | Curry On Functional Programming | Curry On Functional Programming |
|  | 8 iulie | 9 iulie | 10 iulie | 11 iulie | 12 iulie |
| 2-4pm |  |  |  |  |  |
| 4-6pm | You'll Neversea Algorithms Like These |  | REST in Node.JS at the React \& Angular SPA | REST in Node.JS at the React \& Angular SPA |  |
| 6-8pm | Curry On Functional Programming |  |  |  |  |

# Curry On Functional Programming 

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Craiova

## Victor Ciura

Technical Lead, Caphyon
www.caphyon.ro

## Abstract

Can a language whose official motto is "Avoid Success at All Costs" teach us new tricks in modern programming languages?

If Haskell is so great, why hasn't it taken over the world? My claim is that it has. But not as a Roman legion loudly marching in a new territory, rather as distributed Trojan horses popping in at the gates, masquerading as modern features or novel ideas in today's mainstream languages. Functional Programming ideas that have been around for over 40 years will be rediscovered to solve our current software complexity problems.
Indeed, modern programming languages have become more functional. From mundane concepts like lambdas \& closures, function objects, values types and constants, to composability of algorithms, ranges, folding, mapping or even higher-order functions.

In this workshop we'll analyze a bunch of FP techniques and see how they help make our code shorter, clearer and faster, by embracing a declarative vs. an imperative style. Brace yourselves for a bumpy ride including composition, lifting, currying, partial application, pure functions, maybe even pattern matching and lazy evaluation.

Spoiler: no unicorns here.

## Who Am I?



Advanced Installer


Clang Power Tools
¿ @ciura_victor

# Curry On Functional Programming 

## What is it all about?




## Paradox of Programming

Machine/Human impedance mismatch:

- Local/Global perspective
- Progress/Goal oriented
- Detai//Idea
- Vast/Limited memory
- Pretty reliable/Error prone
- Machine language/Mathematics

Is it easier to think like a machine than to do math?

## Semantics

- The meaning of a program
- Operational semantics: local, progress oriented
- Execute program on an abstract machine in your brain
- Denotational semantics
- Translate program to math
- Math: an ancient language developed for humans


## What is Functional Programming?

- Functional programming is a style of programming in which the basic method of computation is the application of functions to arguments
- A functional language is one that supports and encourages the functional style


## Let's address the GNA in the room...

## 》=Haskel L

## A functional language is one that supports and encourages the functional style

## What do you mean?

Summing the integers 1 to 10 in C++/Java/C\#

```
int total = 0;
for (int i = 1; i < 10; i++)
    total = total + i;
```

The computation method is variable assignment.

Summing the integers 1 to 10 in Haskell
sum [1..10]

The computation method is function application.


Sneak Peek Into Next Level QA (Test Automation) - Antonio Valent

## Historical Background



## Historical Background

Most of the "new" ideas and innovations in modern programming languages are actually very old...


## Historical Background

## 1930s



Alonzo Church develops the lambda calculus, a simple but powerful theory of functions

## Historical Background

## 1950s



John McCarthy develops Lisp, the first functional language, with some influences from the lambda calculus, but retaining variable assignments

## Historical Background

## 1960s



Peter Landin develops ISWIM, the first pure functional language, based strongly on the lambda calculus, with no assignments

## Historical Background

## 1970s



John Backus develops FP, a functional language that emphasizes higher-order functions and reasoning about programs

## Historical Background

1970s


Robin Milner and others develop ML, the first modern functional language, which introduced type inference and polymorphic types

## Historical Background

## 1970-80s



David Turner develops a number of lazy functional languages, culminating in the Miranda system

## Historical Background

## 1987



An advanced purely-functional programming language

An international committee starts the development of Haskell, a standard lazy functional language

## Historical Background

## 1990s



Phil Wadler and others develop type classes and monads, two of the main innovations of Haskell

## Historical Background

## 2003 2010



The committee publishes the Haskell Report, defining a stable version of the language; an updated version was published in 2010

## Historical Background

## 2010-2019

- standard distribution

Haskell
Platform
Haskell with batteries included

- library support
- new language features
- development tools
- use in industry
- influence on other languages


## A Taste of Haskell

$$
\begin{aligned}
f[] \quad= & {[] } \\
f(x: x s)= & f \text { ys }++[x]++f \text { zs } \\
& \text { where } \\
& y s=\left[\begin{array}{llll}
a & \mid & a \leftarrow x s, a \leq x
\end{array}\right] \\
& z s=\left[\begin{array}{llll}
b & b \leftarrow x s, b>x
\end{array}\right]
\end{aligned}
$$

What does f do?

## Standard Prelude

Haskell comes with a large number of standard library functions

Select the first element of a list:
> head [1,2,3,4,5]
1

Remove the first element from a list:
> tail [1,2,3,4,5]
[2,3,4,5]

## Standard Prelude

Select the nth element of a list:
> $[1,2,3,4,5]!!2$
3

Select the first $\mathbf{n}$ elements of a list:
> take 3 [1,2,3,4,5]
[1, 2, 3]

## Standard Prelude

Remove the first $\mathbf{n}$ elements from a list:
> drop 3 [1,2,3,4,5]
$[4,5]$

Calculate the length of a list:
> length $[1,2,3,4,5]$
5

Calculate the sum of a list of numbers:
$>\operatorname{sum}[1,2,3,4,5]$
15

## Standard Prelude

Calculate the product of a list of numbers:
> product [1,2,3,4,5]
120
Append two lists:
> $[1,2,3]++[4,5]$
$[1,2,3,4,5]$
Reverse a list:
> reverse [1,2,3,4,5]
[5, $4,3,2,1]$

## Function Application

$$
f a b+c^{*} d
$$



Function application is assumed to have higher priority than all other operators:


## Function Application

| Mathematics | Haskell |
| :--- | :--- |
| $f(x)$ | $f x$ |
| $f(x, y)$ | $f x y$ |
| $f(g(x))$ | $f(g x)$ |
| $f(x, g(y))$ | $f x(g y)$ |
| $f(x) g(y)$ | $f x * g y$ |

## My First Function

$$
\text { double } x=x+x
$$

$$
\text { quadruple } x=\text { double (double } x \text { ) }
$$

> quadruple 10
40
> take (double 2) $[1,2,3,4,5,6]$
[1, 2, 3, 4]

## Infix Functions

## average ns = sum ns `div` length ns

$$
x \text { ` } f^{\prime} y \text { is just syntactic sugar for } f x y
$$

## The Layout Rule

The layout rule avoids the need for explicit syntax to indicate the grouping of definitions

$$
\begin{gathered}
a=b+c \\
\text { where } \\
b=1 \\
c=2 \\
d=a * 2
\end{gathered}
$$

means

$$
\begin{aligned}
a= & b+c \\
& \text { where } \\
& \{b=1 ; \\
& c=2\} \\
d= & a * 2
\end{aligned}
$$

implicit grouping

## Types in Haskell

If evaluating an expression $e$ would produce a value of type $t$,
then e has type $t$, written as $\mathrm{e}:: \mathrm{t}$

Every well formed expression has a type, which can be automatically calculated at compile time using a process called type inference

All type errors are found at compile time,
=> makes programs safer and faster by removing the need for type checks at run time

## List Types

A list is sequence of values of the same type:

$$
\begin{aligned}
& \text { [False,True,False] :: [Bool] } \\
& \text { ['a','b','c','d'] :: [Char] } \\
& \text { [['a'],['b','c']] :: [[Char]] }
\end{aligned}
$$

## Tuple Types

## (False,True) :: (Bool,Bool)

(False, 'a', True) :: (Bool, Char, Bool)
('a',(False,'b')) :: (Char, (Bool,Char))
(True, ['a', 'b']) :: (Bool, [Char])

## Function Types

A function is a mapping from values of one type to values of another type:

$$
\begin{aligned}
& \text { not }:: \text { Bool } \rightarrow \text { Bool } \\
& \text { even }:: \text { Int } \rightarrow \text { Bool }
\end{aligned}
$$

## Function Types

$$
\begin{aligned}
& \text { add }::(\text { Int, Int }) \rightarrow \text { Int } \\
& \text { add }(x, y)=x+y \\
& \text { zeroto }:: \text { Int } \rightarrow[\text { Int }] \\
& \text { zeroto } n=[0 . . n]
\end{aligned}
$$

## Curried Functions

Functions with multiple arguments are also possible by returning functions as results:

$$
\begin{aligned}
& \text { add' }:: \text { Int } \rightarrow \text { (Int } \rightarrow \text { Int) } \\
& \text { add' } x \text { y }=x+y
\end{aligned}
$$

add' takes an integer $\mathbf{x}$ and returns a function add' $\mathbf{x}$ In turn, this new function takes an integer $y$ and returns the result $\mathbf{x}+\mathbf{y}$

## Curried Functions

add and add' produce the same final result, but add takes its two arguments at the same time, whereas add' takes them one at a time:

$$
\begin{aligned}
& \text { add }::(\text { Int, Int }) \rightarrow \text { Int } \\
& \text { add },:: \text { Int } \rightarrow(\text { Int } \rightarrow \text { Int })
\end{aligned}
$$

Functions that take their arguments one at a time are called curried functions, celebrating the work of Haskell Curry on such functions.

## Curried Functions

## Functions with more than two arguments can

 be curried by returning nested functions:$$
\begin{aligned}
& \text { mult : : Int } \rightarrow(\text { Int } \rightarrow(\text { Int } \rightarrow \text { Int })) \\
& \text { mult } x y z=x^{*} y^{*} z
\end{aligned} \begin{aligned}
& \text { mult takes an integer } x \text { and returns a function mult } x \text {, which in } \\
& \text { turn takes an integer } y \text { and returns a function mult } x y \text {, which } \\
& \text { finally takes an integer } z \text { and returns the result } x^{*} y^{*} z
\end{aligned}
$$

## Curried Functions

Curried functions are more flexible than functions on tuples, because useful functions can often be made by partially applying a curried function.

$$
\begin{aligned}
& \text { add' } 1:: \text { Int } \rightarrow \text { Int } \\
& \text { take } 5::[\text { Int }] \rightarrow[\text { Int }] \\
& \text { drop } 5::[\text { Int }] \rightarrow[\text { Int }]
\end{aligned}
$$

## Currying Conventions

To avoid excess parentheses when using curried functions, two simple conventions are adopted:

$$
\text { Int } \rightarrow \text { Int } \rightarrow \text { Int } \rightarrow \text { Int }
$$

The arrow $\rightarrow$ associates to the right

```
same as: Int \(\rightarrow\) (Int \(\rightarrow\) (Int \(\rightarrow\) Int))
```


# Currying Conventions 

As a consequence, it is then natural for function application to associate to the left
mult x y z
means ((mult x) y) z

Unless tupling is explicitly required, all functions in Haskell are normally defined in curried form

## Polymorphic Functions

A function is called polymorphic if its type contains one or more type variables

$$
\text { length :: [a] } \rightarrow \text { Int }
$$

For any type a, length takes a list of values of type a and returns an integer

## Polymorphic Functions

Type variables can be instantiated to different types in different circumstances:

```
> length [False,True]
2
> length [1,2,3,4]
4
```

Type variables must begin with a lower-case letter, and are usually named $a, b, c$...

## Polymorphic Functions

Many of the functions defined in the standard prelude are polymorphic:

$$
\begin{aligned}
& \text { fst }::(a, b) \rightarrow a \\
& \text { head }::[a] \rightarrow a \\
& \text { take }:: \text { Int } \rightarrow[a] \rightarrow[a] \\
& \text { zip }::[a] \rightarrow[b] \rightarrow[(a, b)] \\
& \text { id }:: a \rightarrow a
\end{aligned}
$$

## Guarded Equations

```
abs :: Int }->\mathrm{ Int
abs n = if n \geq 0 then n else -n
```

As an alternative to conditionals, functions can also be defined using guarded equations

$$
\begin{array}{rll}
\text { abs } n & n \geq 0 & n \\
& \mid & \text { otherwise }
\end{array}=-n
$$

## Guarded Equations

```
signum :: Int }->\mathrm{ Int
signum n = if n < 0 then -1 else
    if n == 0 then 0 else 1
```

Guarded equations can be used to make definitions involving multiple conditions easier to read:

$$
\begin{array}{lll}
\text { signum } n & \mathrm{n}<0 & =-1 \\
& \mathrm{n}==0 & =0 \\
& \mid \text { otherwise } & =1
\end{array}
$$

The catch all condition otherwise is defined in the prelude by otherwise = True

# Pattern Matching 

not : : Bool $\rightarrow$ Bool<br>not False = True<br>not True = False

## Pattern Matching

$$
\begin{aligned}
& \text { (\&\&) : : Bool } \rightarrow \text { Bool } \rightarrow \text { Bool } \\
& \text { True \&\& True }=\text { True } \\
& \text { True \&\& False }=\text { False } \\
& \text { False \&\& True }=\text { False } \\
& \text { False \&\& False }=\text { False }
\end{aligned}
$$

can be defined more compactly by:

$$
\begin{aligned}
(\& \&): \text { Bool } & \rightarrow \text { Bool } \rightarrow \text { Bool } \\
\text { True \&\& True } & =\text { True } \\
\text { _ } \quad \& \& \quad & =\text { False }
\end{aligned}
$$

## Pattern Matching

However, the following definition is more efficient, because it avoids evaluating the second argument if the first argument is False

$$
\begin{aligned}
& (\& \&): \text { Bool } \rightarrow \text { Bool } \rightarrow \text { Bool } \\
& \text { True \&\& b }=\text { b } \\
& \text { False \&\& _ }=\text { False }
\end{aligned}
$$

## Pattern Matching

## Patterns are matched in order.

The following definition always returns False:

$$
\begin{aligned}
\quad \& \& & =\text { False } \\
\text { True \&\& True } & =\text { True }
\end{aligned}
$$

## List Patterns

Internally, every non-empty list is constructed by repeated use of an operator $(:)$ called "cons" that adds an element to the start of a list

$$
[1,2,3,4]
$$

means 1:(2:(3:(4:[])))

## List Patterns (x:xs)

Functions on lists can be defined using $X: X S$ patterns

$$
\begin{aligned}
& \text { head :: [a] } \rightarrow \text { a } \\
& \text { head }\left(x: \_\right)=x \\
& \text { tail :: }[a] \rightarrow[a] \\
& \operatorname{tail}(-: x s)=x s
\end{aligned}
$$

x:xs patterns only match non-empty lists:

```
> head []
*** Exception: empty list
```


## Lambda Expressions

$$
\begin{aligned}
& \lambda x \rightarrow x+x \\
& \lambda x \rightarrow x+x
\end{aligned}
$$

the nameless function that takes a number $\mathbf{x}$ and returns the result $\mathbf{x}+\mathbf{x}$

## Lambda Expressions

Lambda expressions can be used to avoid naming functions that are only referenced once

$$
\begin{aligned}
& \text { odds } n=\operatorname{map} f[0 . . n-1] \\
& \text { where } \\
& \qquad f x=x^{*} 2+1
\end{aligned}
$$

can be simplified to:

$$
\text { odds } \mathrm{n}=\operatorname{map}\left(\backslash \mathrm{x} \rightarrow \mathrm{x}^{*} 2+1\right)[0 . . \mathrm{n}-1]
$$

## Set Comprehensions

In mathematics, the comprehension notation can be used to construct new sets from old sets

$$
\left\{x^{2} \mid x \in\{1 \ldots 5\}\right\}
$$

the set $\{1,4,9,16,25\}$ of all numbers $x^{2}$ such that $x$ is an element of the set $\{1 . . .5\}$

## Set Comprehensions

In Haskell, a similar comprehension notation can be used to construct new lists from old lists

$$
[x \wedge 2 \mid x \leftarrow[1 . .5]]
$$

the set $\{1,4,9,16,25\}$ of all numbers $x^{2}$ such that $x$ is an element of the set $\{1 . . .5\}$

## Set Comprehensions

$$
[x \wedge 2 \mid x \leftarrow[1 . .5]]
$$

The expression $x \leftarrow$ [1..5] is called a generator, as it states how to generate values for $x$

Comprehensions can have multiple generators, separated by commas:

$$
\begin{aligned}
& >[(x, y) \mid x \leftarrow[1,2,3], y \leftarrow[4,5]] \\
& {[(1,4),(1,5),(2,4),(2,5),(3,4),(3,5)]}
\end{aligned}
$$

## Set Comprehensions

Changing the order of the generators changes the order of the elements in the final list:

$$
\begin{aligned}
& >[(x, y) \mid y \leftarrow[4,5], x \leftarrow[1,2,3]] \\
& {[(1,4),(2,4),(3,4),(1,5),(2,5),(3,5)]}
\end{aligned}
$$

Multiple generators are like nested loops, with later generators as more deeply nested loops whose variables change value more frequently.

## Set Comprehensions

$$
\begin{aligned}
& >[(x, y) \mid y \leftarrow[4,5], x \leftarrow[1,2,3]] \\
& {[(1,4),(2,4),(3,4),(1,5),(2,5),(3,5)]}
\end{aligned}
$$

$x \leftarrow[1,2,3]$ is the last generator, so the value of the $x$ component of each pair changes most frequently.

## Dependant Generators

Later generators can depend on the variables that are introduced by earlier generators

$$
[(x, y) \mid x \leftarrow[1 . .3], y \leftarrow[x . .3]]
$$

The list $[(1,1),(1,2),(1,3),(2,2),(2,3),(3,3)]$ of all pairs of numbers $(x, y)$ such that $x, y$ are elements of the list [1..3] and $y \geq x$

## Dependant Generators

Using a dependant generator we can define the library function that concatenates a list of lists:

$$
\begin{aligned}
& \text { concat :: [ }[a]] \rightarrow[a] \\
& \text { concat xss }=[x \mid x s \leftarrow x s s, x \leftarrow x s] \\
& \text { > concat }[[1,2,3],[4,5],[6]] \\
& {[1,2,3,4,5,6]}
\end{aligned}
$$

## Guards

List comprehensions can use guards to restrict the values produced by earlier generators

$$
[x \mid x \leftarrow[1 . .10], \text { even } x]
$$

The list $[2,4,6,8,10]$ of all numbers $x$ such that $\mathbf{x}$ is an element of the list [1..10] and $\mathbf{x}$ is even

## Guards

Using a guard we can define a function that maps a positive integer to its list of factors:

```
    factors :: Int -> [Int]
    factors n = [x | x \leftarrow [1..n], n `mod` x == 0]
> factors 15
[1,3,5,15]
```


## Guards

A positive integer is prime if its only factors are 1 and itself. Using factors we can define a function that decides if a number is prime:

$$
\begin{aligned}
& \text { prime }:: \text { Int } \rightarrow \text { Bool } \\
& \text { prime } n=\text { factors } n==[1, n]
\end{aligned}
$$

> prime 15
False
> prime 7
True

## Guards

Using a guard we can now define a function that returns the list of all primes up to a given limit:

$$
\begin{aligned}
& \text { primes }:: \text { Int } \rightarrow \text { [Int }] \\
& \text { primes } n=[x \text { | } \mathrm{x} \leftarrow[2 \ldots \mathrm{n}] \text {, prime } \mathrm{x}]
\end{aligned}
$$

> primes 40

$$
[2,3,5,7,11,13,17,19,23,29,31,37]
$$

## Zip Function

A useful library function is zip, which maps two lists to a list of pairs of their corresponding elements

$$
\text { zip }::[a] \rightarrow[b] \rightarrow[(a, b)]
$$

> zip ['a','b','c'] [1,2,3,4]
[('a',1), ('b', 2), ('c', 3)]

## Zip Function

Using zip we can define a function returns the list of all pairs of adjacent elements from a list:

$$
\begin{aligned}
& \text { pairs : : }[a] \rightarrow[(a, a)] \\
& \text { pairs xs }=\text { zip xs (tail xs) }
\end{aligned}
$$

> pairs $[1,2,3,4]$
$[(1,2),(2,3),(3,4)]$

## Zip Function

Using pairs we can define a function that decides if the elements in a list are sorted:

```
sorted :: Ord a = [a] -> Bool
sorted xs = and [x \leq y | (x,y) \leftarrow pairs xs]
> sorted [1,2,3,4]
True
> sorted [1,3,2,4]
False
```


## String Comprehensions

A string is a sequence of characters enclosed in double quotes. Internally, however, strings are represented as lists of characters.

```
"abc" :: String
```

means ['a', 'b', 'c'] :: [Char]

## String Comprehensions

Because strings are just special kinds of lists, any polymorphic function that operates on lists can also be applied to strings.

```
> length "abcde"
5
> take 3 "abcde"
"abc"
> zip "abc" [1,2,3,4]
[('a',1),('b',2),('c',3)]
```


## String Comprehensions

List comprehensions can also be used to define functions on strings, such counting how many times a character occurs in a string:
count : : Char $\rightarrow$ String $\rightarrow$ Int
count $x$ xs $=$ length [ $\left.x ’ \mid x ’ \leftarrow x s, x==x^{\prime}\right]$
> count 'e' "Open4Tech Summer School"
3

## Recursive Functions

$$
\begin{aligned}
& \text { fac } 0=1 \\
& \text { fac } n=n * \text { fac }(n-1)
\end{aligned}
$$

## Recursive Functions

$$
\text { product }[2,3,4]
$$

$$
2 \text { * product }[3,4]
$$

$$
\begin{aligned}
& \text { product }:: \text { Num } a \Rightarrow[a] \rightarrow a \\
& \text { product }[] \quad=1 \\
& \text { product }(n: n s)=n * \text { product ns }
\end{aligned}
$$

$$
2 *(3 * \text { product [4]) }
$$

$$
2 \text { * (3 * (4 * product [])) }
$$

$$
2 *(3 *(4 * 1))
$$

24

## Recursive Functions

$$
\begin{aligned}
& \text { length }[1,2,3] \\
& 1+\text { length }[2,3] \\
& 1+(1+\text { length [3]) } \\
& 1+(1+(1+\text { length }[])) \\
& 1+(1+(1+0)) \\
& 3
\end{aligned}
$$

## Recursive Functions

```
reverse :: [a] -> [a]
reverse [] = []
reverse (x:xs) = reverse xs ++ [x]
```

reverse $[1,2,3]$
reverse $[2,3]++[1]$
(reverse [3] ++ [2]) ++ [1]
((reverse [] ++ [3]) ++ [2]) ++ [1]
$(([]++[3])++[2])++[1]$
$[3,2,1]$

## Recursive \& Multiple Args

$$
\begin{aligned}
& \operatorname{zip}::[a] \rightarrow[b] \rightarrow \\
& \operatorname{zip}[(a, b)] \\
& \operatorname{zip} \overline{[ } \overline{[]}=[] \\
& \operatorname{zip}(x: x s)(y: y s)=[] \\
&(x, y): \text { zip xs ys }
\end{aligned}
$$

## Recursive \& Multiple Args

$$
\begin{aligned}
& \text { drop :: Int } \rightarrow[a] \rightarrow[a] \\
& \text { drop } 0 \text { xs } \\
& \text { drop }-[] \\
& \text { drop } \bar{n}(-: x s) \\
& \text { d } \\
& =[]
\end{aligned}
$$

## Recursive \& Multiple Args

$$
\begin{array}{ll}
(++): & {[a] \rightarrow[a] \rightarrow[a]} \\
{[]} & ++y s=y s \\
(x: x s) & ++ \text { ys }=x:(x s++y s)
\end{array}
$$

## Quick Sort

Rules:

1. The empty list is already sorted.
2. Non-empty lists can be sorted by sorting the tail values $\leq$ the head, sorting the tail values > the head, and then appending the resulting lists on either side of the head value.

## Quick Sort

$$
\left.\begin{array}{l}
\text { qsort : : Ord } a \Rightarrow[a] \rightarrow[a] \\
\text { qsort }[]=[] \\
\text { qsort }(x: x s)= \\
\text { qsort smaller }++[x]++ \text { qsort larger } \\
\text { where } \\
\text { smaller }
\end{array}\right]\left[\begin{array}{lll}
a & \mid a \leftarrow x s, a \leq x] \\
\text { larger } & =[b \mid b \leftarrow x s, b>x]
\end{array}\right.
$$

## Quick Sort



## Higher-Order Functions

A function is called higher-order if it takes a function as an argument or returns a function as a result.

$$
\begin{aligned}
& \text { twice }::(a \rightarrow a) \rightarrow a \rightarrow a \\
& \text { twice } f x=f(f x)
\end{aligned}
$$

## Higher-Order Functions

Common programming idioms can be encoded as functions within the language itself.
Domain specific languages can be defined as collections of higher-order functions.
Algebraic properties of higher-order functions can be used to reason about programs.

## Higher-Order Functions

Give me examples from your favorite programming language/library

# Higher-Order Functions 

## Map

$$
\begin{aligned}
& \text { map }::(a \rightarrow b) \rightarrow[a] \rightarrow[b] \\
> & \operatorname{map}(+1)[1,3,5,7] \\
& {[2,4,6,8] }
\end{aligned}
$$

## Map Function

The map function can be defined in a simple manner using a list comprehension:

$$
\operatorname{map} f x s=[f \times \mid x \leftarrow x s]
$$

Alternatively, the map function can also be defined using recursion:

$$
\begin{array}{ll}
\operatorname{map} f[] & =[] \\
\operatorname{map} f(x: x s) & =f x: \operatorname{map} f x s
\end{array}
$$

## Filter Function

The higher-order function filter selects every element from a list that satisfies a predicate

$$
\begin{aligned}
& \text { filter }::(a \rightarrow B o o l) \rightarrow[a] \rightarrow[a] \\
> & \text { filter even }[1 . .10] \\
& {[2,4,6,8,10] }
\end{aligned}
$$

## Filter Function

Filter can be defined using a list comprehension:

$$
\text { filter } p \text { xs }=[\mathrm{x} \mid \mathrm{x} \leftarrow \mathrm{xs}, \mathrm{p} \mathrm{x}]
$$

Alternatively, it can be defined using recursion:

```
filter p [] = []
filter p (x:xs)
    | p x = x : filter p xs
    | otherwise = filter p xs
```


## Foldr Function

A number of functions on lists can be defined using the following simple pattern of recursion:

$$
\begin{array}{ll}
f[] & =v \\
f(x: x s) & =x \oplus f x s
\end{array}
$$

f maps the empty list to some value $\mathbf{v}$, and any non-empty list to some function $\oplus$ applied to its head and $f$ of its tail

## Foldr Function

$$
\begin{array}{ll}
\operatorname{sum}[] & =0 \\
\text { sum }(x: x s)=x+\text { sum } x s & \\
& =0 \\
\text { product [] }=1 & \\
\text { product }(x: x s)=x^{*} \text { product } x s & \\
& \\
\text { and }[] & =\text { True }
\end{array}
$$

## Foldr Function

The higher-order library function foldr (fold right) encapsulates this simple pattern of recursion, with the function $\oplus$ and the value $v$ as arguments

$$
\begin{aligned}
& \text { sum }=\text { foldr (+) } 0 \\
& \text { product }=\text { foldr (*) } 1 \\
& \text { or }=\text { foldr (||) False } \\
& \text { and }=\text { foldr (\&\&) True }
\end{aligned}
$$

## Foldr Function

It is best to think of foldr as simultaneously replacing each (: ) in a list by a given function, and [] by a given value

$$
\begin{aligned}
& \operatorname{sum}[1,2,3] \\
= & \text { foldr }(+) 0[1,2,3] \\
= & \text { foldr }(+) 0(1:(2:(3:[]))) \\
= & 1+(2+(3+0)) \\
= & 6
\end{aligned}
$$

> | replace each ( E |
| :--- |
| by $(+)$ and $\overline{\mathrm{l}}$ by 0 |

## Foldr Function

It is best to think of foldr as simultaneously replacing each (: ) in a list by a given function, and [] by a given value

```
_product [1,2,3]
= foldr (*) 1 [1,2,3]
= foldr (*) 1 (1:(2:(3:[])))
=
    1*(2*(3*1))
=
6
```

replace each (:) by (*) and $\mathbb{\square}$ by 1

## Foldr Function

$$
\begin{aligned}
\text { length :: }[a] & \rightarrow \text { Int } \\
\text { length }[] & =0 \\
\text { length }\left(\_: x s\right) & =1+\text { length xs }
\end{aligned}
$$

length $=$ foldr $(\backslash \quad n \rightarrow 1+n) 0$

## Foldr Function

$$
\begin{aligned}
\text { reverse :: }[a] & \rightarrow[a] \\
\text { reverse }[] & =[] \\
\text { reverse }(x: x s) & =\text { reverse xs ++ }[x]
\end{aligned}
$$

```
reverse = foldr (\x xs -> xs ++ [x]) []
```


## Foldr Function

Some recursive functions on lists, such as sum, are simpler to define using foldr.
Properties of functions defined using foldr can be proved using algebraic properties of foldr Advanced program optimizations can be simpler if foldr is used in place of explicit recursion

## Function Composition

The library function (.) returns the composition of two functions as a single function

$$
\begin{aligned}
& (.)::(b \rightarrow c) \rightarrow(a \rightarrow b) \rightarrow(a \rightarrow c) \\
& f . g=\lambda x \rightarrow f(g x)
\end{aligned}
$$

Eg.

$$
\begin{aligned}
& \text { filter: }:(a->B o o l)->[a]->[a] \\
& \text { length: }:[a]->\text { Int } \\
=> & \\
& \text { let } e=\text { length . filter }(\backslash x \rightarrow>\text { odd } x) \times s \\
& e: \text { Int }
\end{aligned}
$$

## Functional Patterns in C++

## Problem:

## Counting adjacent repeated values in a sequence.

How many of you solved this textbook exercise before? (in any programming language)


## $\mathbf{C + +}$ Counting adjacent repeated values in a sequence

$$
\{5,8,8,2,1,1,9,4,4,7\}
$$

Who wants to try it now?


## C++ Counting adjacent repeated values in a sequence

Visual hint:

$$
\begin{aligned}
& \quad\{5,8,8,2,1,1,9,4,4,77\} \\
& \\
& \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \\
& \quad\{5,8,8,2,1,1,9,4,4,7\} \\
& \\
& \quad=\quad \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \\
& \quad\{0,1,0,0,1,0,0,1,0\}
\end{aligned}
$$

## C++ Counting adjacent repeated values in a sequence

Let me guess... a bunch of for loops, right?

How about something shorter?
An STL algorithm maybe?

## $\mathbf{C + +}$ Counting adjacent repeated values in a sequence

```
template<class InputIt1, class InputIt2,
    class T,
    class BinaryOperation1, class BinaryOperation2>
T inner_product(InputIt1 first1, InputIt1 last1,
    InputIt2 first2, T init,
    BinaryOperation1 op1 // "sum" function
    BinaryOperation2 op2) // "product" function
{
    while (first1 != last1)
    {
        init = op1(init, op2(*first1, *first2));
        ++first1;
        ++first2;
        }
        return init;
}

\section*{\(\mathbf{C + +}\) Counting adjacent repeated values in a sequence}
```

template <typename T>
int count_adj_equals(const T \& xs) // requires non-empty range
{
return std::inner_product(
std::cbegin(xs), std::cend(xs) - 1, // to penultimate elem
std::cbegin(xs) + 1, // collection tail
0,
std::plus{},
std::equal_to{}); // yields boolean => 0 or 1
}

```

\section*{\(\mathbf{C + +}\) Counting adjacent repeated values in a sequence}

If you found that piece of code in a code-base, would you understand what it does* ?

* without my cool diagram \& animation

\title{
Counting adjacent repeated values in a sequence
}

Let's go back to Haskell for a few minutes...


\section*{Counting adjacent repeated values in a sequence}

Visual hint:
\[
\begin{aligned}
& {[5,8,8,2,1,1,9,4,4, \square 7]} \\
& \downarrow \downarrow \downarrow \downarrow \downarrow \\
& {[5,8,8,2,1,1,9,4,4,7]} \\
& (-) \downarrow \downarrow \downarrow \\
& {[-3,0,6,1,0,-8,5,0,-3](==0) \square 3}
\end{aligned}
\]

\section*{Counting adjacent repeated values in a sequence}
\[
\begin{aligned}
& \text { let xs = [ 5, 8, 8, 2, 1, 1, 9, 4, 4, 7] } \\
& \text { count_if } f=\text { length . filter } f \\
& \text { adj_diff = mapAdjacent (-) } \\
& \text { count_adj_equals = count_if }(==0) \text {. adj_diff } \\
& \text { > count_adj_equals xs } \\
& 3
\end{aligned}
\]

Counting adjacent repeated values in a sequence Let's break it down:
\[
\begin{aligned}
& \text { // C++ } \\
& \text { [] (auto a, auto b) \{ return } a+b ;\} \\
& \text { plus\{\} } \\
& \text { // Haskell } \\
& \text { ( } \backslash a b->a+b \text { ) } \\
& \text { (+) } \\
& \text { ( } \backslash e \text {-> e == 1) } \\
& \text { ( }==1 \text { ) }
\end{aligned}
\]

Lambdas \& sections

Counting adjacent repeated values in a sequence Let's break it down:
\[
\begin{aligned}
& \text { length::[a] -> Int } \\
& \text { filter::(a->Bool) -> [a] -> [a] } \\
& \text { => } \\
& \text { count_if::(a->Bool) -> [a] -> Int } \\
& \text { count_if } \mathrm{f}=\text { length . filter f }
\end{aligned}
\]

Counting adjacent repeated values in a sequence
Let's break it down:
\[
\begin{aligned}
& \text { mapAdjacent:: }(a->a->b) \text {-> }[a] \text {-> }[b] \\
& \text { mapAdjacent } \overline{[] ~=~[] ~} \\
& \text { mapAdjacent } \mathrm{f} \text { xs }=\text { zipWith f xs (tail xs) }
\end{aligned}
\]
```

(-)::a -> a -> a
adj_diff = mapAdjacent (-)
=>
adj_diff::[a] -> [a]

```

Counting adjacent repeated values in a sequence Let's break it down:
\[
\begin{aligned}
& (==0):: a \text {-> Bool } \\
& \text { count_if::(a->Bool) -> [a] -> Int } \\
& \text { adj_diff::[a] -> [a] }
\end{aligned}
\]
count_adj_equals::[a] -> Int count_adj_equals = count_if (==0) . adj_diff

Counting adjacent repeated values in a sequence Let's break it down:
\[
\begin{aligned}
& \text { let xs }=[5,8,8,2,1,1,9,4,4,7] \\
& >\text { let ds }=\text { adj_diff xs } \\
& {[-3,0,6,1,0,-8,5,0,-3]} \\
& >\text { count_if(==0) ds } \\
& 3
\end{aligned}
\]

\title{
Counting adjacent repeated values in a sequence
}

\author{
The algorithm
}
\[
\begin{aligned}
& \text { count_if } f=\text { length . filter } f \\
& \text { adj_diff }=\text { mapAdjacent }(-) \\
& \text { count_adj_equals }=\text { count_if }(==0) \text {. adj_diff }
\end{aligned}
\]
\(\mathbf{C + +}\) Counting adjacent repeated values in a sequence

\section*{Back to modern C++}
template <typename T>
int count_adj_equals(const T \& xs)
\{
return accumulate(0, zip(xs, tail(xs)) | transform(equal_to\{\}));
\}

\section*{C++20 Ranges}

\section*{Homework}

1986:
Donald Knuth was asked to implement a program for the "Programming pearls" column in the Communications of ACM journal.

The task:
Read a file of text, determine the n most frequently used words, and print out a sorted list of those words along with their frequencies.

\section*{His solution written in Pascal was 10 pages long.}

\section*{Homework}

Response by Doug Mcllroy was a 6-line shell script that did the same:
\[
\begin{gathered}
\text { tr -cs A-Za-z '\n' | } \\
\text { tr A-Z a-z | } \\
\text { sort | } \\
\text { uniq -c | } \\
\text { sort -rn | } \\
\text { sed } \$\{1\} q
\end{gathered}
\]

\section*{Homework}

Taking inspiration from Doug Mcllroy's UNIX shell script, write a C++ or Haskell algorithm, that solves the same problem: word frequencies

\section*{It's all about pipelines !}

\section*{C++ 20 Ranges}

Print only the even elements of a range in reverse order:
```

std::for_each(
std::crbegin(v), std::crend(v),
[](auto const i) {
if(is_even(i))
cout << i;
});

```
```

for (auto const i : v
| rv::reverse
| rv::filter(is_even))
{
cout << i;
}

```

\section*{C++ 20 Ranges}

Skip the first \(\mathbf{2}\) elements of the range and print only the even numbers of the next \(\mathbf{3}\) in the range:
```

auto it = std::cbegin(v);
std::advance(it, 2);
auto ix = 0;
while (it != cend(v) \&\& ix++ < 3)
{
if (is_even(*it))
cout << (*it);
it++;
}

```
for (auto const \(i\) : v
    | rv::drop(2)
    | rv::take(3)
    | rv::filter(is_even))
\(\{\)
    cout << i;
\}

\section*{C++ 20 Ranges}

Modify an unsorted range so that it retains only the unique values but in reverse order.
```

vector<int> v{ 21, 1, 3, 8, 13, 1, 5, 2 };
std::sort(std::begin(v), std::end(v));
v.erase(
std::unique(std::begin(v), std::end(v)),
std::end(v));
std::reverse(std::begin(v), std::end(v));

```

\section*{C++ 20 Ranges}

Create a range of strings containing the last 3 numbers divisible to 7 in the range [101, 200], in reverse order.

















\section*{C++ 20 Ranges}

\section*{Until the new ISO standard lands in a compiler near you...}

\section*{Eric Niebler's implementation of the Ranges library is available here: \\ https://github.com/ericniebler/range-v3}

It works will Clang 3.6.2 or later, gcc 5.2 or later, and MSVC 15.9 or later.

Although the standard namespace for the Ranges library is std::"ranges, in this current implementation of the library it is ranges::v3
\[
\begin{aligned}
& \text { namespace } r s=r a n g e s:: v 3 ; \\
& \text { namespace } r v=r a n g e s:: v 3:: v i e w ; \\
& \text { namespace } r a=r a n g e s:: v 3:: \text { action; }
\end{aligned}
\]

\section*{Higher-Order Functions}

\section*{Higher Order Functions for Ordinary C++ Developers}

\author{
Björn Fahller \\ compose([](auto const\& s) \{ return s = "foo"; \(\}\), std::mem_fn(\&foo:: name)) \\ https://github.com/rollbear/lift
}
https://www.youtube.com/watch?v=qL6zUn7iiLg

\section*{Higher-Order Functions}

\section*{boost: :hof}

\author{
https://www.boost.org/doc/libs/develop/libs/hof/doc/html/doc/
}

\section*{Further Study}
"Ranges for distributed and asynchronous systems"
- Ivan Čukić [ACCU 2019]
https://www.youtube.com/watch?v=eelpmWo2fuU
"C++ Algorithms in Haskell and the Haskell Playground"
- Conor Hoekstra [C++Now 2019]
https://www.youtube.com/watch?v=dTO3-1C1-t0


\author{
"Functional Programming in C++" - Ivan Čukić
}
https://www.amazon.com/Functional-Programming-programs-functional-techniques/dp/1617293814


\section*{Historical Background}

\section*{1990s}


Phil Wadler and others develop type classes and monads, two of the main innovations of Haskell

\section*{Takeaway}

"Make your code readable.
Pretend the next person who looks at your code is a psychopath and they know where you live."

Phil Wadler

\title{
Curry On Functional Programming
}

July, 2019
Craiova

\section*{Victor Ciura}

Technical Lead, Caphyon
www.caphyon.ro```

